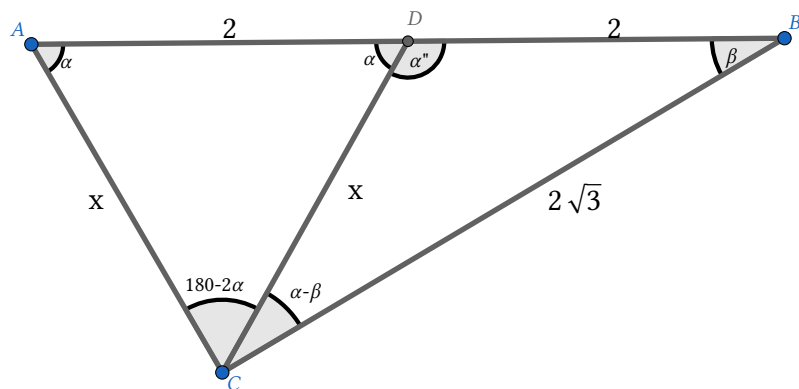


022-PISAREK



$$|CD| = |AC| \quad |AD| = |DB| \quad |AB| = 4 \quad |BC| = 2\sqrt{3}$$

wyznaczyć α, β, γ

$$\alpha, \beta, \gamma \in (0^\circ, 180^\circ)$$

$$\text{niech } x = |AC| \quad x \in \mathbb{R}_+$$

z twierdzenia cosinusów dla $\triangle DBC$ i $\triangle ABC$:

$$\begin{cases} x^2 = 4 + 12 - 8\sqrt{3} \cos \beta \\ x^2 = 16 + 12 - 16\sqrt{3} \cos \beta \end{cases}$$

$$x^2 = 4$$

$$x = 2 \vee x = -2 \notin \mathbb{R}_+$$

$$x = 2, \text{ zatem } \alpha = 60^\circ, \beta = 30^\circ, \gamma = 90^\circ$$